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Fifth Semester B.E. Degree Examination, January/February 2005
Electrical & Electronics Engineering
Digital Signal Processing

Time: 3 hrs.]

[Max.Marks : 100

Note: Answer any FIVE full questions.

1. (a) Compute the N - point DFT of the sequences.

i) $x(n) = a^n \quad 0 \leq n < N - 1$

ii) $x(n) = 1$ for n even
 0 for n odd

(10 Marks)

- (b) Determine 8 point DFT of the sequence

$$x(n) = [1, 1, 1, 1, 1, 1, 0, 0]$$

Sketch its magnitude and phase spectra.

(10 Marks)

2. (a) Consider the two four point sequences given below.

$$x(n) = \cos \frac{\pi n}{2} \quad 0 < n < 3$$

$$h(n) = 2^n \quad 0 < n < 3$$

Calculate $y(n) = x(n) \otimes h(n)$. Use matrix method.

(8 Marks)

- (b) Compute 4 point circular convolution of the sequences given by

$$x(n) = [1, 0, 5] \quad h(n) = [0, 5, 1]$$

Using DFT and IDFT method.

(12 Marks)

3. (a) Given $x(n) = [0, 1, 2, 3, 4, 5, 6, 7]$ find $X(k)$ using DIT-FFT algorithm.

(12 Marks)

- (b) Compute DFT of the sequence $x(n) = \cos \frac{n\pi}{2}$ where $N = 4$ using DIF - FFT algorithm.

(8 Marks)

4. (a) A linear time - variant system is described by the following input - output relation.

$$2y(n) - y(n - 2) - 4y(n - 3) = 3x(n - 2)$$

Realize the system in the following form

- i) Direct form I realization

- ii) Direct form II realization.

(8 Marks)

- (b) Obtain a cascade realisation for the system function given below.

$$H(z) = \frac{(1+Z^{-1})^3}{(1-\frac{1}{4}Z^{-1})(1-Z^{-1}+\frac{1}{2}Z^{-2})} \quad (6 \text{ Marks})$$

- (c) Realize a linear phase FIR filter with the following impulse response

$$h(n) = \delta(n) + \frac{1}{2}\delta(n-1) - \frac{1}{4}\delta(n-2) + \delta(n-4) + \frac{1}{2}\delta(n-3) \quad (6 \text{ Marks})$$

5. (a) Consider an FIR filter having the system function

$$H(Z) = 1 + Z^{-1} + Z^{-2} + \dots + Z^{-(N-1)}$$

Deduce a realization for this FIR filter so that there are only two additions and no multiplications but N delay elements. (8 Marks)

- (b) Explain the principal features of the Harvard architecture. (6 Marks)

- (c) Explain Bilinear transformation method of digital filter design. (6 Marks)

6. (a) A second order analog filter has repeated poles at $s = -a$ transform filter to digital domain, using impulse invariance mapping method. (6 Marks)

- (b) Apply impulse variance transformation to the analog transfer function.

$$H(s) = \frac{e}{s^2 + As + B} \text{ to digital domain.} \quad (8 \text{ Marks})$$

- (c) Convert the analog filter with system function $H(s) = \frac{s+a}{(s+a)^2 + b^2}$ into digital filter impulse response by the use of the bilinear mapping technique. (6 Marks)

7. Design an IIR filter that when used in the prefilter $A/D-H(z)-D/A$ structure will satisfy the following equivalent analog specifications.

i) LPF with -1 dB cut off at $100\pi \text{ rad/sec}$

ii) Stopband attenuation of 35dB at $1000\pi \text{ rad/sec}$

iii) Monotonic stopband and pass band

iv) Sampling rate of 2000 samples/sec. Use Bilinear transform. (20 Marks)

8. (a) Design a LPF with approximate frequency response given below using rectangular window.

$$H_d(e^{j\omega}) = \begin{cases} 1 & \omega \leq \frac{\pi}{2} \\ 0 & \frac{\pi}{2} \leq |\omega| \leq \pi \end{cases}$$

Take $M = 11$, find the values of $h(n)$. (10 Marks)

- (b) The desired frequency response of LPF is

$$H_d(e^{j\omega}) = \begin{cases} e^{-j3\omega} & -\frac{3\pi}{4} \leq \omega \leq \frac{3\pi}{4} \\ 0 & -\frac{3\pi}{4} \leq |\omega| \leq \pi \end{cases}$$

Design using Hamming window $M = 7$

Also obtain frequency response.

(10 Marks)

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